

Quanta and Particles in Quantum Field Theory

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- ▶ Nonrelativistic QM, with or without interactions, can likewise be reformulated as a field theory and the duality is likewise exact

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- ▶ Haag's theorem rigorously establishes that there is no unitary equivalence between free and interacting representations of a field theory (Earman, D.Fraser)
- ▶ Particles and fields don't match 1:1 in the Standard Model (Bain)
- ▶ The duality relies on a decoupling of fields into uncoupled oscillators that just doesn't hold

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- ▶ Occasionally you hear that particles don't exist
- ▶ Mostly, philosophers say that particles are *emergent*
- ▶ But what — at the level of formal structure — are these emergent entities?

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- ▶ Requires UV cutoff to be well-defined and IR cutoff to circumvent Haag's theorem, but that's okay

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 - ▶ No field (in the Hamiltonian) associated with the proton, pion, etc.

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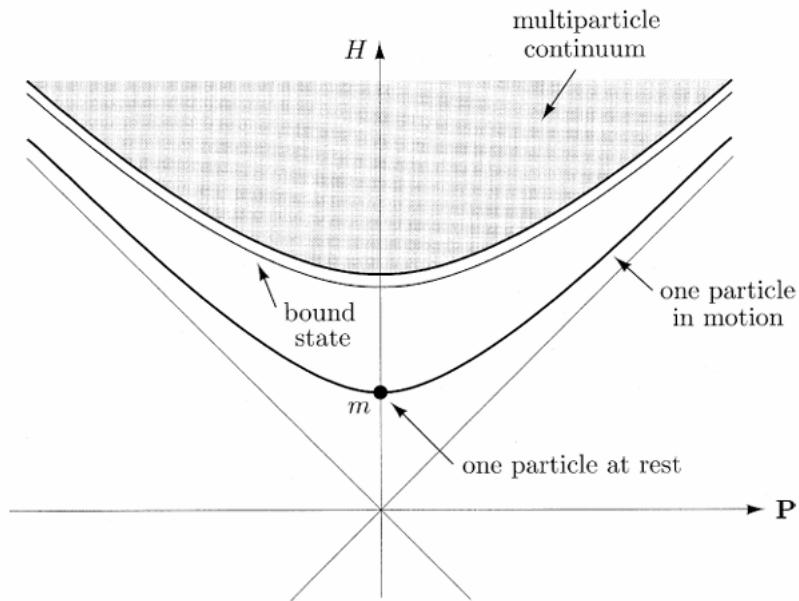
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- ▶ (Boltzmann regime in statistical mechanics and kinetic theory)

(Peskin and Schroeder p.213)



Single-particle states

If f is a function on spacetime approximately localized at event x and with Fourier transform overlapping with a particle mass shell but no other occupied region, then (up to normalization)

$$\hat{a}_f^\dagger |\Omega\rangle = \int dx^4 f(x) \hat{\phi}(x) |\Omega\rangle$$

is a 1-particle state (of that particle),

$$\hat{a}_f^\dagger |\Omega\rangle \propto \int \frac{dk^3}{(2\pi)^3 2\omega_k} \tilde{f}(\mathbf{k}, \omega_k) |\mathbf{k}\rangle$$

Multiparticle states

If f_1, \dots, f_n are N such functions localized at events x_1, \dots, x_n all at some (finite!) time t_i and separated by $\gg 1/m$, then (via the Cluster Decomposition Theorem) up to exponentially small corrections,

$$|f_1, \dots, f_n\rangle \equiv \hat{a}_{f_n}^\dagger \cdots \hat{a}_{f_1}^\dagger |\Omega\rangle$$

will behave as an n -particle state as long as the wavepackets remain non-overlapping

Scattering (I)

If we similarly construct a state $|g_1, \dots, g_m\rangle$ describing an m -particle state at a later time, then

$$\langle g_1, \dots, g_m | f_1, \dots, f_n \rangle$$

is the scattering amplitude between the two states and can be expressed in terms of the $n + m$ -point function,

$$\langle g_1, \dots, g_m | f_1, \dots, f_n \rangle \propto$$

$$\int dx^{4m} dy^{4n} \mathcal{G}(x_1, \dots, x_m, y_1, \dots, y_n) g_1(x_1) \cdots g_m(x_m) f_1(y_1) \cdots f_n(y_n)$$

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- ▶ Spatially narrower wavepackets can resolve scale effects in interactions, e.g. long-lived resonances, long(er)-range forces

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- ▶ Method: *effective field theory*. Write down the most general nonrelativistic theory of electrons and photons and evaluate the coefficients by matching to QED cross-sections.
- ▶ (Resultant theory is non-unitary in some circumstances, e.g. electron/positron annihilation)

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Conclusions

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- ▶ The quanta of perturbed harmonic oscillators provide a useful but very thin notion of particle — to thin to do all the work that ‘particle’ does in physics
- ▶ Much more robust notions are available through scattering theory and nonrelativistic EFT
- ▶ These notions are approximate and domain-dependent, but non-perturbative